Feedforward neural networks

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Summary

Feedforward neural networks for text classification

Gradient descent

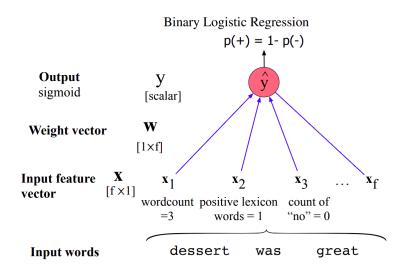
Feedforward neural networks for language modeling

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Feedforward neural networks for text classification

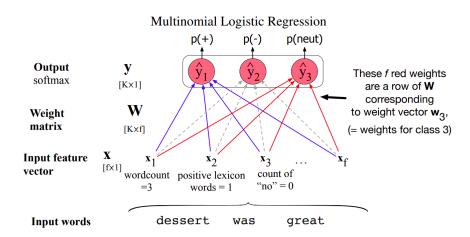
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Binary logistic regression



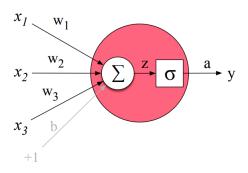
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Multinomial logistic regression



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Neural unit



$$y = \sigma(w \cdot x + b) = \frac{1}{1 + \exp(-(w \cdot x + b))}$$

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Activation functions

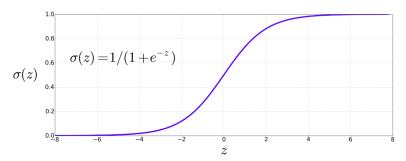
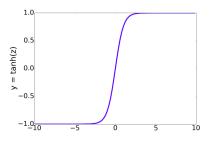


Figure: Sigmoid function.

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Activation functions



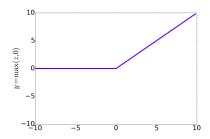
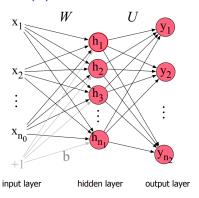


Figure: Tanh and ReLU functions.

$$y = \tanh(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$
$$y = \text{ReLU}(z) = \max(z, 0)$$

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Feedforward network (1)



$$h = \sigma(Wx + b)$$

$$z = Uh$$

$$y = \text{softmax}(z)$$

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Feedforward network (2)

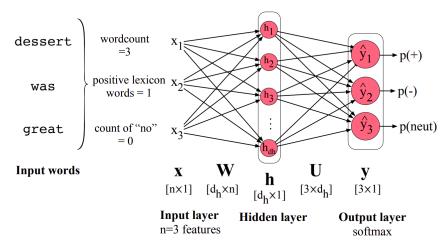


Figure: Feedforward network sentiment analysis using traditional hand-built features.

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Feedforward network (3)

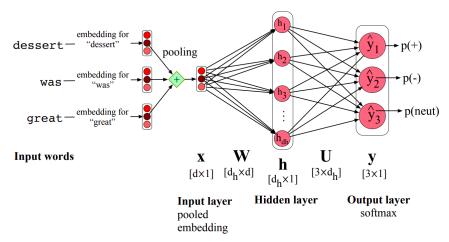


Figure: Feedforward network sentiment analysis using a pooled embedding.

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Without activation functions, a multi-layer NN is equivalent to a single-layer NN $\,$

Consider the first two layers of a neural network with purely linear transformations:

$$z^{[1]} = W^{[1]}x + b^{[1]}$$

 $z^{[2]} = W^{[2]}z^{[1]} + b^{[2]}$

The operations performed by the network can be combined and simplified as follows:

$$z^{[2]} = W^{[2]}(W^{[1]}x + b^{[1]}) + b^{[2]}$$

$$= W^{[2]}W^{[1]}x + W^{[2]}b^{[1]} + b^{[2]}$$

$$= W_0x + b_0$$

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Gradient descent

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Loss function

The loss function for a single example x in the context of a multi-class classification problem, with K output classes, is defined as the cross-entropy loss L_{CE} :

$$L_{CE}(\hat{y}, y) = -\sum_{k=1}^{K} y_k \log(\hat{y}_k)$$

The loss L_{CE} for a prediction \hat{y} and true label y, focusing on the correct class c, is represented as:

$$\begin{aligned} L_{CE}(\hat{y}, y) &= -\log(\hat{y}_c) \\ &= -\log\left(\frac{\exp(z_c)}{\sum_{j=1}^K \exp(z_j)}\right) \end{aligned}$$

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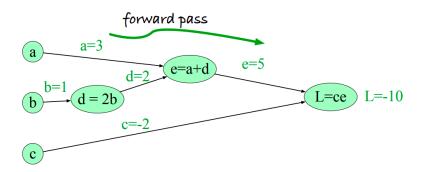
Computing the gradients

For deep networks, computing the gradients for each weight is difficult, since we are computing the derivative with respect to weight parameters that appear all the way back in the very early layers of the network

The solution to computing this gradient is an algorithm called *error* backpropagation

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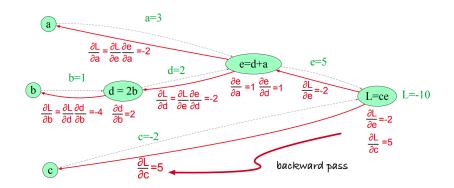
Forward pass



$$L(a,b,c)=c(a+2b)$$

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Backward pass



$$L(a,b,c)=c(a+2b)$$

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Backpropagation calculus, 3Blue1Brown's video https://www.youtube.com/watch?v=Ilg3gGewQ5U

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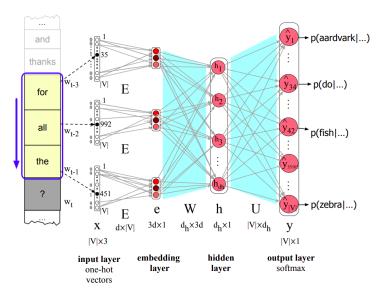
A feedforward neural language model takes as input at time t a representation of some number of previous words (w_{t-1}, w_{t-2} , etc.) and outputs a probability distribution over possible next words

Like the n-gram, it approximates the probability of a word given the entire prior context by approximating based on the n-1 previous words:

$$P(w_t|w_1,...,w_{t-1}) \approx P(w_t|w_{t-N+1},...,w_{t-1})$$

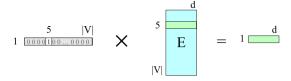
Unlike n-gram models, neural language models generalize better over contexts of similar words, and are more accurate at word prediction

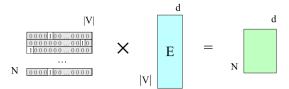
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Embedding





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The equations for a neural language model with a *window size* of 3, given *one-hot input vectors* for each context word, are:

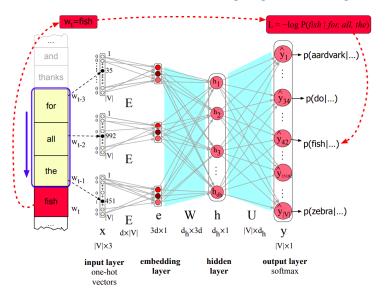
$$e = [Ex_{t-3}; Ex_{t-2}; Ex_{t-1}]$$

$$h = \sigma(We + b)$$

$$z = Uh$$

$$\hat{y} = \text{softmax}(z)$$

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How to improve the training?

Find good **hyperparameters**: batch size, learning rate, activation functions, number of hidden layers, number of neural units

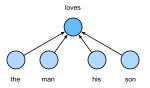
Apply **regularization** methods: normalize input values, add dropout, add weight decay

Other techniques include label smoothing, cutting gradients norm, augmenting data, using good weights initialization, gradient descent with momentum (Adam optimizer), etc.

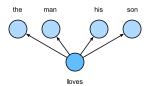
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Skip-gram and Continuous Bag-of-Words models

Continuous Bag-of-Words:



Skip-gram:



Self-supervised models with window size of 2 Learned classifier weights are word embeddings

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Exercices

Using PyTorch, you need to:

- Implement logistic regression
- ► Implement multi-layer feedforward network for text classification based on word2vec and tf-idf features
- ► Implement multi-layer feedforward network for language modeling
- Play with hyperparameters
- ► Implement skip-gram or continuous bag-of-words models (optional)

The goal is to have a workable PyTorch training loop for your project!

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